

# Microscopy

- It magnifies the objective
- see the virtual image of the object.
- Diffraction and absorption is necessary for image formation.

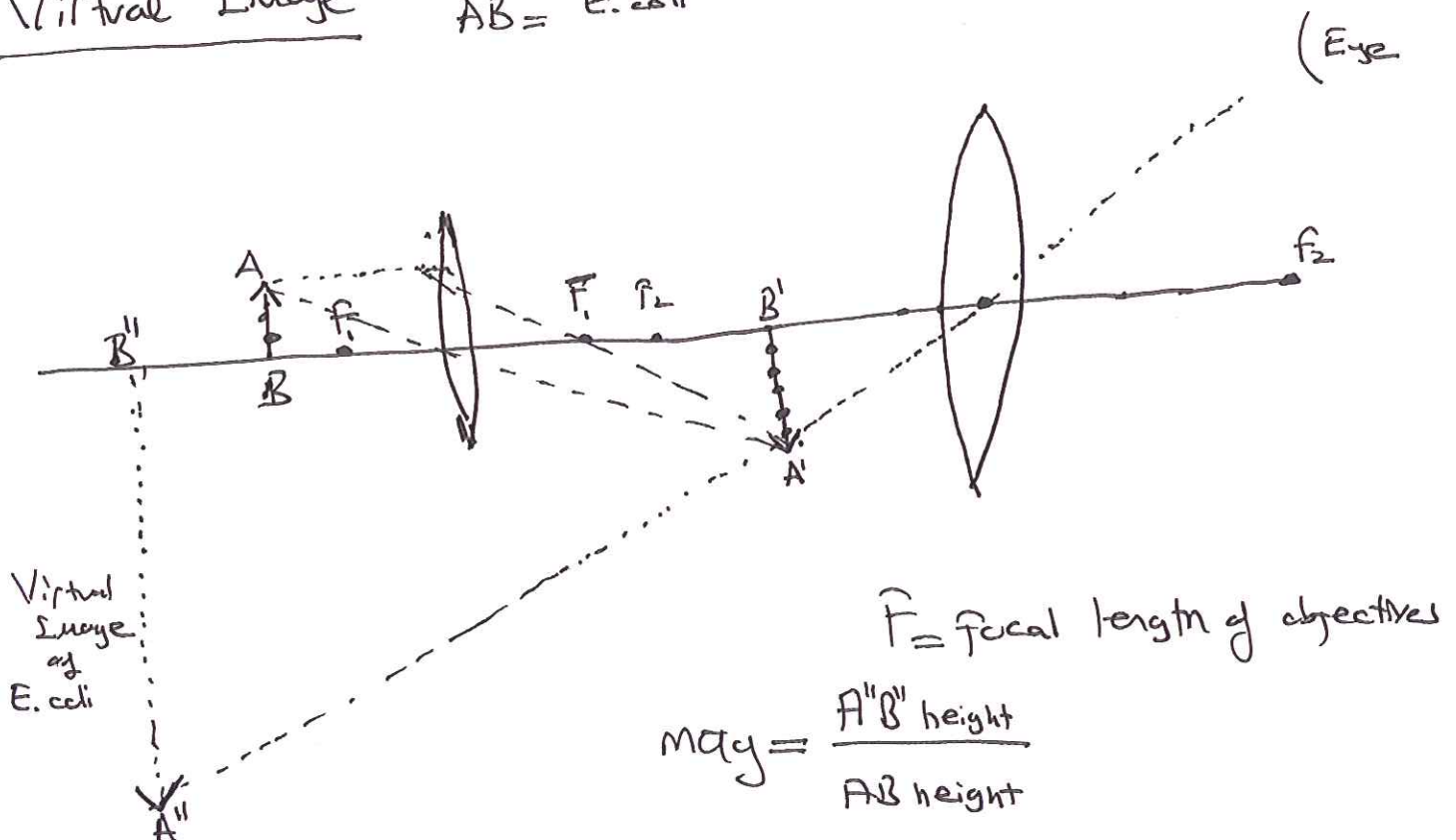
$$\text{Magnification} = \frac{\text{Virtual size by the objective}}{\text{Real size of the object}}$$

For example,  $\frac{0.5 \text{ cm}}{2 \mu\text{m E. coli}} = 2500 \text{ times magnification}$

$60\times$  by objective  $\times$   $20\times$  by eyepiece or binocular  $\times$   $2$  times by microscope  $\cong 2400$  times mag.

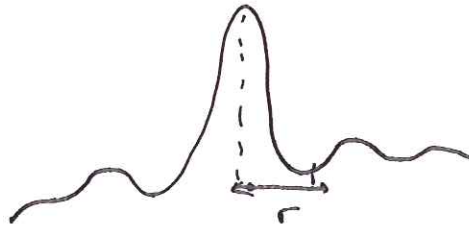
$$\text{Mag} = \text{Mag}_{\text{objective}} \times \text{Mag}_{\text{binocular/eyepiece}}$$

## Virtual Image AB = E. coli

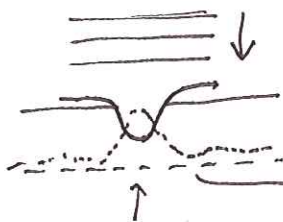


# Resolution of the microscope

$$r_{\text{airy}} = \frac{1.22 \lambda}{2 NA \sin \theta}$$



$$d = \frac{\lambda}{2 NA} = \frac{\lambda}{2 n \sin \theta}$$

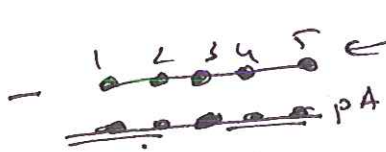


Bending of light by diffraction

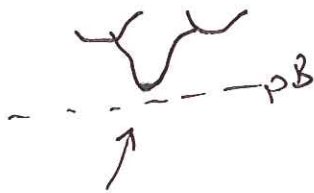
Destructive

Constructive (Constructive)

## Huygens' principle



light can be represented by many point like sources.

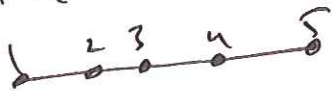


At point A = all waves contribute the same direction and amplitude

All 5 sources contribute.

at point B

only 1, 2, 3 and wave from 4 and 5 contribute.



$$\text{at point A} = \psi(A) = \psi_1 + \psi_2 + \psi_3 + \psi_4 + \psi_5$$

for ex,

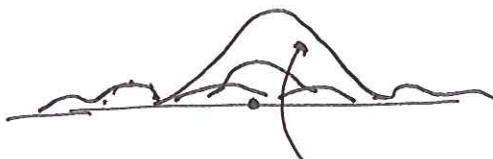
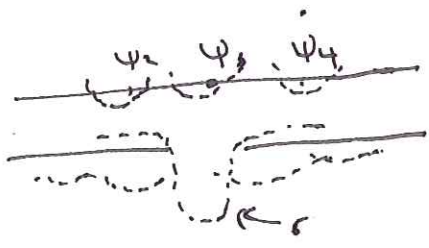


Constructive Interference.

$$\text{at point B} = \psi(B) = \cancel{\psi_1} + \psi_2 + \psi_3 + \psi_4 + \psi_5$$

Dark (Destructive Interference)

$$r = \frac{0.61 \lambda}{NA}$$



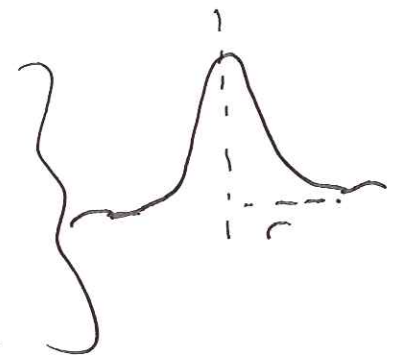
All point source waves contribute to the formation of the central peak.

$$\text{Resulting Pulse} = \psi_2 + \psi_3 + \psi_4$$

$$\psi_2 = \text{[small positive pulse]}$$

$$\psi_3 = \text{[small negative pulse]}$$

$$\psi_4 = \text{[small positive pulse]}$$



- Numerical Aperture:  
 - Range of angles collected of light collected by the objective (lens)  
 $NA = n \sin \theta$

$NA = 0.87$  if  $n = 1.52$

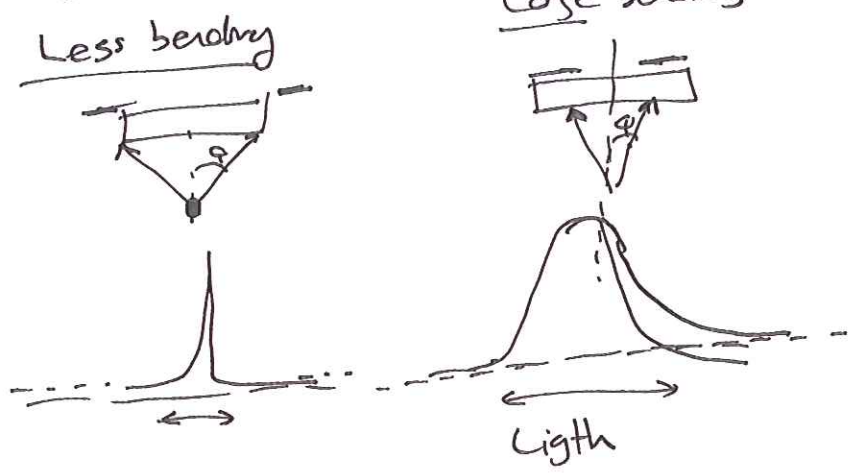
$NA = 0.12$  if  $n = 1.00$

$n =$  index of refraction

Air = 1.00

Ditto = 1.33

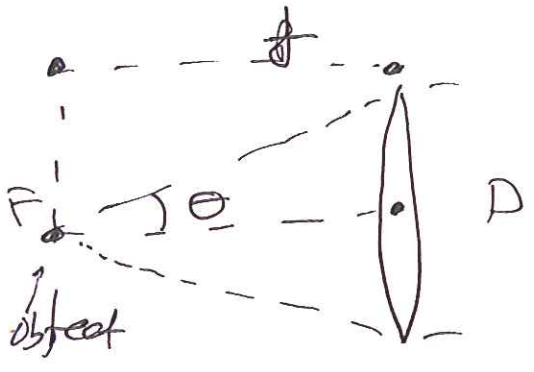
Oil = 1.52



Light pass a large slit and therefore less bending and diffraction occurs.

If NA is small, that means it is a smaller slit and large diffraction occurs.

- it has no dimension



$NA = n \times \sin \theta$

$N = \frac{F}{D}$  } photography  
 they use f-number

$$\underbrace{\text{Mag (obj)} \times 0.61 \times \frac{\lambda}{NA}} = 2.3 \times \text{pixel size}$$

$$\frac{10 \mu\text{m}}{2} \approx 5 \mu\text{m} \text{ pixel size required}$$

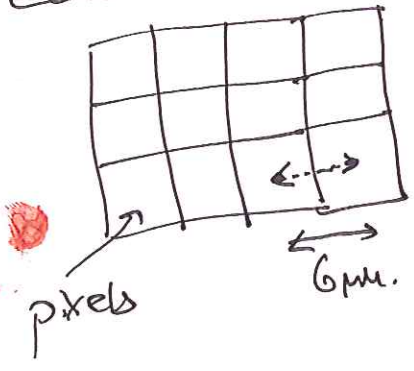
⇒ Sampling interval (pixel size) required adequately reconstruct an analogue signal must be at least twice the maximum frequency measured.

$$\text{pixel frequency} \geq \frac{\text{Sampling frequency}}{2}$$

Numerical

### Camera Pixel Size

Ander - 6μm  
Covered



$$0.61 \times \frac{480}{1.4} \times 60x \approx 12 \mu\text{m}$$

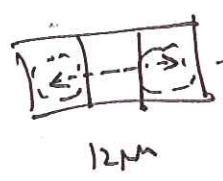
$$A = 209 \text{ nm}$$

$$12 = 2.3 \times \text{pixel size}$$

$$\text{Pixel size} = 5.2 \mu\text{m}$$

If you use Ander, you may have the true resolution of 209 nm.

⇒ you can resolve two objects if their separation is small as 209 nm.



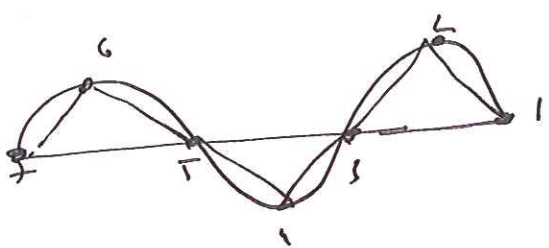


Nyquist theorem.

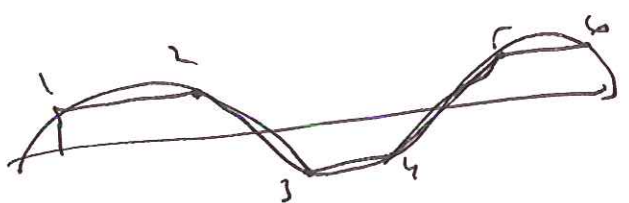
To reconstruct an analog signal

for example;  $f_{xy} = \frac{0.6 \times 1}{1.2} = \frac{0.6 \times 10000}{1.2} = 20000$  theoretical resolution

pixel size =  $\frac{20000}{2} = 10000$



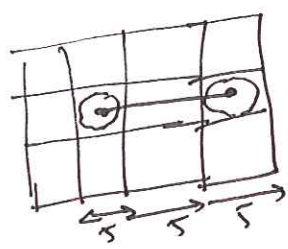
$f = 10$  kHz,  
frequency of recording  $\geq 2 \times f$  sample.



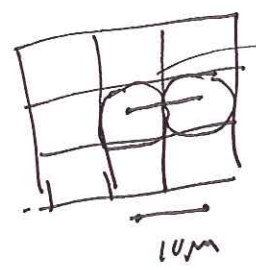
In microscopy:

Size of the pixel should be two times smaller than size of Magnified object.

10  $\mu m$  object magnified, small, largest pixel size  $\approx 5 \mu m$



what if you have a smaller & large size pixel?



you can not separate the object with a large pixel size camera.

Recording frequency  $\geq 2 \times$  Sample size

Pixel are used to identify objects.